

### Homework Topic 13 (Due Thursday 5/19)

1.
  - a. Sketch two different functions whose derivative is  $y' = 4$ . In each case; give the rule for the original function and check the derivative is  $y' = 4$ .
  - b. How many possible functions satisfy this requirement?
  - c. Suppose  $y(1) = 3$  and  $y' = 4$ ; what is the original function now?
  - d. Sketch  $y' = 4$  and the function you determined in part c) together.
  
2.
  - a. Sketch two different functions whose derivative is  $y' = -4x$ . In each case; give the rule for the original function and check the derivative is  $y' = -4x$ .
  - b. How many possible functions satisfy this requirement?
  - c. Suppose  $y(-1) = 8$  and  $y' = -4x$ ; what is the original function now?
  - d. Sketch  $y' = -4x$  and the function you determined in part c) together.
  
3.
  - a. Sketch two different functions whose derivative is  $y' = 3x^2 + 1$ . In each case; give the rule for the original function and check the derivative is  $y' = 3x^2 + 1$ .
  - b. How many possible functions satisfy this requirement?
  - c. Suppose  $y(0) = 1$  and  $y' = 3x^2 + 1$ ; what is the original function now?
  - d. Sketch  $y' = 3x^2 + 1$  and the function you determined in part c) together.